Study of mesoscopic behaviour of light in disordered and gain-loss assisted systems from application point of view

A Thesis submitted by **Sayan Bhattacherjee**

in partial fulfillment of the requirements for the award of the degree of **Doctor of Philosophy**



Indian Institute of Technology Jodhpur Physics April, 2023

Certificate

This is to certify that the thesis titled Study of mesoscopic behaviour of light in disordered and gain-loss assisted systems from application point of view, submitted by Sayan Bhattacherjee (P17PH005) to the Indian Institute of Technology Jodhpur for the award of the degree of Doctor of Philosophy, is a bonafide record of the research work done by him under my supervision. To the best of my knowledge, the contents of this report, in full or in parts, have not been submitted to any other Institute or University for the award of any degree or diploma.

> Dr. Somnath Ghosh Ph.D.Thesis Supervisor

Sourattistrach

Declaration

I hereby declare that the work presented in this thesis entitled *Study of mesoscopic behaviour of light in disordered and gain-loss assisted systems from application point of view* submitted to the Indian Institute of Technology Jodhpur in partial fulfillment of the requirements for the award of the degree of Doctor of Philosophy, is a bonafide record of the research work carried out under the supervision of Dr. Somnath Ghosh. The contents of this thesis in full or in parts, have not been submitted to, and will not be submitted by me to, any other Institute or University in India or abroad for the award of any degree or diploma.

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Sayan Bhattacherjee

Dedicated to my brother

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List of abbreviations

Abbreviation Full form

MSD Mean squared displacement

RMS Root mean square

DL Dynamic Localization

NNTB Nearest-neighbor tight-binding

FWHM Full width at half maximum

TAL Transverse Anderson localization

PT Parity-Time

MFP Mean free path

eMSD Ensemble averaged mean squared displacement

COM Center of mass

PDF Probability density function

AAH Abry-André-Harper

SSH Su–Schrieffer–Heeger

PMMA Polymethyl methacrylate